

## Part III: Hardy-Weinberg Problems

### Remember:

$p$  = dominant allele /  $q$  = recessive allele

$p^2$  = homozygous dominant individuals

$2pq$  = heterozygous individuals

$q^2$  = homozygous recessive individuals

$$p^2 + 2pq + q^2 = 1$$

$$p + q = 1$$

1. Let's say that brown fur coloring is dominant to gray fur coloring in mice. If you have 168 brown mice in a population of 200 mice then . . . .

a. What is the predicted frequency of heterozygotes?  $2pq = 2(0.6)(0.4) = 0.48$

b. What is the predicted frequency of homozygous dominant?  $p^2 = (0.6)^2 = 0.36$

c. What is the predicted frequency of homozygous recessive  $q^2 = (0.4)^2 = 0.16$

$$q = 0.4 \quad p = 0.6$$

2. The allele for the hair pattern called "widow's peak" is dominant over the allele for no "widow's peak". In a population of 1,000 individuals, 510 show the dominant phenotype. How many individuals would you expect of each of the possible three genotypes for this trait?

$q = 0.7$        $p = 0.3$       **Homozygous Dominant:  $p^2 = (0.3)^2 = 0.09 \times 100 = 90$  individuals**

**Heterozygous:  $2pq = 2(0.3)(0.7) = 0.42 \times 100 = 420$  individuals**

**Homozygous Recessive:  $q^2 = (0.7)^2 = 0.49 \times 100 = 490$  individuals**

3. In the United States about 16% of the population is Rh negative. The allele for Rh negative is recessive to the allele for Rh positive. If the student population of a high school in the U.S. is 2,000, how many students would you expect for each of these three possible genotypes?

$q = 0.4$        $p = 0.6$       **Homozygous Dominant:  $p^2 = (0.6)^2 = 0.36 \times 2000 = 720$  individuals**

**Heterozygous:  $2pq = 2(0.6)(0.4) = 0.48 \times 2000 = 960$  individuals**

**Homozygous Recessive:  $q^2 = (0.4)^2 = 0.16 \times 2000 = 320$  individuals**

4. In certain African countries 4% of the newborn babies have sickle cell anemia, which is a recessive trait. Out of a random population of 1,000 newborn babies, how many would you expect for each of the three possible genotypes?

**$q = 0.2$        $p = 0.8$       Homozygous Dominant:  $p^2 = (0.8)^2 = 0.64 \times 1000 = 640$  individuals**  
**Heterozygous:  $2pq = 2(0.8)(0.2) = 0.32 \times 1000 = 320$  individuals**  
**Homozygous Recessive:  $q^2 = (0.2)^2 = 0.04 \times 1000 = 40$  individuals**

5. In a certain population, the dominant phenotype of a certain trait occurs 91% of the time. What is the frequency of the dominant allele?

**$p = 0.7$**

6. A very large population of randomly-mating laboratory mice contains 25% white mice. White coloring is caused by the double recessive genotype, "aa". Calculate allelic and genotypic frequencies for this population.

**Allelic Frequencies**

**$q = 0.5$        $p = 0.5$**

**Genotypic Frequencies**

**Homozygous Dominant:  $p^2 = (0.5)^2 = 0.25$**

**Heterozygous:  $2pq = 2(0.5)(0.5) = 0.50$**

**Homozygous Recessive:  $q^2 = (0.5)^2 = 0.25$**

7. In Drosophila (fruit fly), the allele for normal wing length is dominant over the allele for short wings. In a population of 1000 individuals, 360 show the recessive phenotype. How many individuals would you expect to be homozygous dominant for the trait.

**$q = 0.6$        $p = 0.4$       Homozygous Dominant:  $p^2 = (0.4)^2 = 0.16 \times 1000 = 160$  individuals**

8. The allele for a widow's peak (hairline) is dominant over the allele for a straight hairline. In a population of 500 individuals, 9% show the recessive phenotype. How many individuals would you expect to be homozygous dominant and heterozygous for the trait?

**$q = 0.3$        $p = 0.7$       Homozygous Dominant:  $p^2 = (0.7)^2 = 0.49 \times 500 = 245$  individuals**  
**Heterozygous:  $2pq = 2(0.7)(0.3) = 0.42 \times 500 = 210$  individuals**

9. In a given population, only the "A" and "B" alleles are present in the ABO system; there are no individuals with type "O" blood or with O alleles in this particular population. If 200 people have type A blood, 75 have type AB blood, and 25 have type B blood, what are the allelic frequencies of this population?

	Frequency of A allele	Frequency of B allele
200 AA - Homozygous	$\frac{(200 \times 2) + (75 \times 1)}{600}$	$\frac{(25 \times 2) + (75 \times 1)}{600}$
75 AB - Heterozygous	600	600
+25 BB - Homozygous		
300	$\frac{475}{600}$	$\frac{125}{600}$
<u>x 2</u>	600	600
600 alleles	$0.792 = 0.8$	$0.208 = 0.2$

10. In Mr. Collea's AP Biology class at North Salem High School, \_\_\_\_ members of the class have free earlobes. Free earlobes are controlled by the dominant gene "F" and attached earlobes are controlled by the recessive gene "f." Determine the **allelic frequencies** (p and q) along with the **number of individuals** you would expect to have each of the possible three genotypes for this trait?

	Phenotypes				Allele Frequency Based on the H-W Equation	
	Free Earlobes (p <sup>2</sup> + 2pq)		Attached Earlobes (q <sup>2</sup> )		p	q
	#	%	#	%		
<b>Class Population</b>						
<b>North American Population</b>	0.45		0.55			



Free Earlobes

Attached Earlobes